JASWANT MODERN SR. SEC.SCHOOL SUMMER HOLIDAY WORKSHEET 2025-26 MATHS CLASS 10

- 1. If HCF (26,169) = 13, find the LCM (26,169).
- 2. If a and b are co-prime numbers, then find the HCF(a,b).
- 3. Express 156 and 126 as the product of primes
- **4.** Prove that $3 + 2\sqrt{5}$ is irrational, if we given that $\sqrt{5}$ is irrational.
- **5.** If two positive integers p and q can be expressed $p = ab^2$ and $q = a^3b$; a, b being prime numbers, then LCM (p, q).
- **6.** Show that 12ⁿ cannot end with digit 0 or 5 for any natural number n .
- 7. Prove that $\sqrt{2}$ and $\sqrt{5}$ is irrational.
- **8.** If HCF (26,169) = 13, find the LCM (26,169)
- 9. Find a quadratic polynomial, the sum and product of whose zeroes are -1/4 and 1/4.
- **10.** If α and β are the zeroes of the polynomial $x^2 5x + k$, such that $\alpha \beta = 1$. Find k.
- 11. If α and β are the zeroes of the polynomial $2x^2 5x + 7$, find polynomial whose zeroes are $2\alpha + 3$ and $2\beta + 3$
- 12. If α and β are the zeroes of the polynomial $x^2 4x + k$, show that $\alpha + \beta 2\alpha\beta = 4$. find the value of k.
- 13. Find the zeroes of the polynomial $x^2 +7x +10$ and verify the relationship between the zeroes and the coefficients.
- **14.** If α and β are the zeroes of the polynomial $3x^2 + 7x + 5$, find a polynomial whose zeroes are 3α and 3β .
- **15.** Find the zeroes of the polynomial $6x^2$ 3- 7x and verify the relationship between the zeroes and the coefficients.
- **16.** If α and β are the zeros of quadratic polynomial $p(x) = x^2 x 4$, find the value of $(\alpha + \beta)^2 2\alpha\beta$
- 17. Find the quadratic polynomial, the sum of whose zeroes is 0 and one zero is 4.
- **18.** If α and β are the zeroes of the polynomial $2x^2 13x + 6$, then $\alpha + \beta$
- **19.** if x = -1/2 is a solution of the quadratic equation $3x^2 + 2kx 3 = 0$, find the value of k.
- **20.** if the quadratic equation $px^2 2\sqrt{5}px + 15 = 0$ has two equal roots, then find the value of P.
- 21. which of the following is not quadratic equation?
 - (i) $x(2x+3) = x^2+1$
- (ii) $(x+2)^3 = x^3 4$
- (iii) $(x+2)^2 = x^2$
- 22. Find the discriminant of the Quadratic equation $2x^2 4x + 3 = 0$ and hence find the nature of its roots.
- 23. find the roots of the quadratic equation $x^2 + 5x 14 = 0$
- **24.** solve for x: $\sqrt{2x+9} + x = 13$ by:
 - by factorisation
- **25.** solve for x : $4x^2 + 4bx (a^2 b^2) = 0$
 - by quadratic formula
- **26.** solve for x : $\sqrt{3}$ x² $2\sqrt{2}$ x $2\sqrt{3}$ = 0 by quadratic formula
- 27. find the value of k for which the equation $2x^2 (k-1)x + 8 = 0$ will have real and equal roots.
- **28.** if the roots of the equation $(a b)x^2 + (b c)x + (c a) = 0$ are equal, prove that 2a = b + c find the positive values of k which
- **29.** equations $x^2 + kx + 64 = 0$ and $x^2 8x + k = 0$ both will have real roots.
- **30.** The angle of the elevation of the top of a tower from the point of a ground which is 30 m away from the foot of a tower, is 30° . Find the height of the tower.
- 31. A statue 1.6 m tall stands on the top of a pedestal. From a point on the ground, the angle of the elevation on the top of the statue is 60° and the same point the angle of elevation of the top of the pedestal is 45° . Find the height of the pedestal.
- **32.** As observed from the top of a 75 m tall lighthouse, the angle of depression of two ships are 30° and 45° . If one ship is exactly behind the other on the same side of the lighthouse, find the distance between the two ships
- 33. From a point on a bridge across a river, the angles of depression of the banks on opposite sides of the river are 30° and 45° , respectively. If the bridge is at a height of 3 m from the banks, find the width of the river.
- **34.** The shadow of a tower standing on a level ground is found to be 40 m longer when the Sun's altitude is 30° than when it is 60° . Find the height of the tower.
- **35.** At a point A, 20 m above the level of water in a lake, the angle of the elevation of a cloud is 30° . The angle of depression of the reflection of the cloud in the lake, at A is 60° . Find the distance of the cloud from A.
- **36.** A cloud tower stands on a horizontal plane and is surmounted by a vertical flagstaff of height h. At a point on the plane, the angle of elevation of the bottom and the top of the flagstaff are α and β , prove that the height of tower is $\frac{h \tan \alpha}{\tan \beta \tan \alpha}$.
- 37. A man standing on the deck of a ship, which is 10 m above the water level, observes the angle of elevation of the top of a hill as 60° and the angle depression of the base of the hill as 30° . find the distance of the hill from the ship and the height of the hill.

- **38.** A straight highway leads to the foot of a tower. A man standing at the top of the tower observes a car at the angle depression of 30° , which is approaching to the foot of the tower with a uniform speed. Six seconds later, the angle of the depression of the car is found to be 60° . Find the time taken by the car to the reach the foot of the tower.
- **39.** From a point P on the ground the angle of elevation of the top of a 10 m tall building is 30°. A flag is hoisted at the top of the building and the angle of elevation of the top of the flagstaff from P is 45°. Find the length of the flagstaff and the distance of the building from the point P.

An observer 1.5 m tall is 28.5 m away from a chimney. The angle of elevation of the top of the chimney from her eyes is 45°. What is the height of the chimney?

- **40.** The angles of depression of the top and the bottom of an 8 m tall building from the top of a multistoried building are 30° and 45°, respectively. Find the height of the multistoried building and the distance between the two buildings.
- **41.** The angles of elevation of the top of a tower from two points at a distance of 4 m and 9 m from the base of the tower and in the same straight line with it are complementary. Prove that the height of tower is 6 m.
- **42.** A 1.2 m tall girl spots a balloon moving with the wind in a horizontal line at a height of 88.2 m from the ground. The angle of elevation of the balloon from the eyes of the girl at any instant is 60°. After some time, the angle of elevation reduces to 30°. Find the distance travelled by the balloon during the interval.
- **43.** A TV tower stands vertically on a bank of a canal. From a point on the other bank directly opposite the tower, the angle of elevation of the top of the tower is 60°. From another point 20 m away from this point on the line joining this point to the foot of the tower, the angle of elevation of the top of the tower is 30°. Find the height of the tower and the width of the canal.
- 44. One card is drawn from a well-shuffled deck of 52 cards. Find the probability of getting
 - (i) a king of red colour (ii) a face card
- **45.** In a play zone, Amit is playing claw crane game which consist of 58 teddy bears, 42 Pokémon's, 36 tigers and 64 monkeys. Amit picks a puppet at random. now
 - 1. Find the probability of getting a tiger.
- 2. Find the probability of getting a monkey.
- 3. Find the probability of getting not a monkey
- 4. Find the probability of getting not a Pokémon
- 46. Two coins are tossed simultaneously. What is the probability of getting
 - (a) At least one head?
- (b) At most one tail?
- (c) A head and a tail?
- 47.Two dice are thrown simultaneously, find the probability of getting:
 - i) An even number as the sum:
- ii). A doublets:
- iii) An odd number as the sum: